

TEXT BOOK EXERCISE 8.3

Q. 1. Multiply each of the following pairs :

- (i) $4x, x + y$
- (ii) $(x - 3y), x^2$
- (iii) $(x + y), 7xy$
- (iv) $(x^2 - 9x), 4x$
- (v) $(a + b), 0$
- (vi) $(ab + bc), ab$

Solution.

$$(i) \quad 4x \times (x + y) = (4x \times x) + (4x \times y) \\ = 4x^2 + 4xy \text{ Ans.}$$

$$(ii) \quad (x - 3y) \times x^2 = x^2 \times (x - 3y) \\ = (x^2 \times x) + (x^2) (- 3y) \\ = x^3 - 3x^2y \text{ Ans.}$$

$$(iii) \quad (x + y) \times 7xy = 7xy \times (x + y) \\ = (7xy \times x) + (7xy \times y) \\ = 7x^2y + 7xy^2 \text{ Ans.}$$

$$(iv) \quad (x^2 - 9x) \times 4x = 4x \times (x^2 - 9x) \\ = (4x \times x^2) + (4x \times -9x) \\ = 4x^3 - 36x^2 \text{ Ans.}$$

$$(v) \quad (a + b) \times 0 = 0(a + b) \\ = (0 \times a) + (0 \times b) \\ = 0 + 0 = 0 \text{ Ans.}$$

$$(vi) \quad (ab + bc) \times ab = (ab) \times (ab + bc) \\ = (ab \times ab) + (ab \times bc) \\ = a^2b^2 + ab^2c \text{ Ans.}$$

Q. 2. Complete the table

First expression	Second expression	Product
(i) $a^2b^2c^2$	$ab + bc + ca$	
(ii) $x + y + z$	$2xy$	
(iii) $p + q - 2r$	$2p$	
(iv) $b + c - a$	abc	

Solution. (i) $a^2b^2c^2 \times (ab + bc + ca)$
 $= (a^2b^2c^2 \times ab) + (a^2b^2c^2 \times bc) + (a^2b^2c^2 \times ca)$
 $= a^3b^3c^2 + a^2b^3c^3 + a^3b^2c^3 \text{ Ans.}$

$$(ii) \quad (x + y + z) \times (2xy) \\ = 2xy \times (x + y + z) \\ = (2xy \times x) + (2xy \times y) + (2xy \times z) \\ = 2x^2y + 2xy^2 + 2xyz \text{ Ans.}$$

$$(iii) \quad (p + q - 2r) \times 2p \\ = 2p \times (p + q - 2r) \\ = (2p \times p) + (2p \times q) + (2p \times -2r) \\ = 2p^2 + 2pq - 4pr \text{ Ans.}$$

$$(iv) \quad b + c - a \times abc \\ = abc \times (b + c - a) \\ = (abc \times b) + (abc \times c) + (abc \times -a) \\ = ab^2c + abc^2 - a^2bc \text{ Ans.}$$

Q. 3. Find the Product of :

- (i) a^2 and $(a^2 - b^2)$
- (ii) $4xy$ and $(-2x - 3y)$
- (iii) a and $(a^2 - 2ab + b^2)$
- (iv) $4x^2$ and $(-x^2 - y^2 + 2x)$

Solution.

$$\begin{aligned} (i) \quad & a^2 \times (a^2 - b^2) \\ &= (a^2 \times a^2) + (a^2 \times -b^2) \\ &= a^4 - a^2 b^2 \text{ Ans.} \end{aligned}$$

$$\begin{aligned} (ii) \quad & 4xy \times (-2x - 3y) \\ &= (4xy \times -2x) + (4xy \times -3y) \\ &= -8x^2 y - 12xy^2 \text{ Ans.} \end{aligned}$$

$$\begin{aligned} (iii) \quad & a \times (a^2 - 2ab + b^2) \\ &= (a \times a^2) + (a \times -2ab) + (a \times b^2) \\ &= a^3 - 2a^2 b + ab^2 \text{ Ans.} \end{aligned}$$

$$\begin{aligned} (iv) \quad & 4x^2 \times (-x^2 - y^2 + 2x) \\ &= (4x^2 \times -x^2) + (4x^2 \times -y^2) \\ &\quad + (4x^2 \times 2x) \\ &= -4x^4 - 4x^2 y^2 + 8x^3 \text{ Ans.} \end{aligned}$$

Q. 4. Simplify the following and find its value with the given value of the variable

$$(i) \quad x(3x + 2) - 7 \text{ if } x = 1 \text{ and } x = \frac{1}{2}$$

$$(ii) \quad y(2y^2 - 7y) + 8 \text{ if } y = 0 \text{ and } y = -1$$

$$(iii) \quad xy(x^2y - xy^2) \text{ if } x = 1, y = 2$$

$$(iv) \quad ab(a + ab + abc) \text{ for } a = 2, b = 1, c = 0$$

Solution.

$$(i) \quad x(3x + 2) - 7 = 3x^2 + 2x - 7 \text{ Ans.}$$

For $x = 1$,

$$\begin{aligned} 3x^2 + 2x - 7 &= 3(1)^2 + 2(1) - 7 \\ &= 3 + 2 - 7 = -2 \text{ Ans.} \end{aligned}$$

For $x = \frac{1}{2}$,

$$\begin{aligned} 3x^2 - 2x - 7 &= 3\left(\frac{1}{2}\right)^2 + 2 \times \frac{1}{2} - 7 \\ &= 3 \times \frac{1}{4} + 1 - 7 = \frac{3}{4} - 6 \\ &= \frac{3 - 24}{4} = -\frac{21}{4} \text{ Ans.} \end{aligned}$$

$$\begin{aligned} (ii) \quad & xy(x^2y - xy^2) \\ &= (xy \times x^2y) + (xy \times -xy^2) \\ &= x^3y^2 - x^2y^3 \text{ Ans.} \end{aligned}$$

For $x = 1, y = 2$,

$$\begin{aligned} x^3y^2 - x^2y^3 &= (1)^3 (2)^2 - (1)^2 (2)^3 \\ &= 1 \times 4 - 1 \times 8 \\ &= 4 - 8 = -4 \text{ Ans.} \end{aligned}$$

$$(iii) \quad y(2y^2 - 7y) + 8 = 2y^3 - 7y^2 + 8 \text{ Ans.}$$

For $y = 0$,

$$\begin{aligned} 2y^3 - 7y^2 + 8 &= 2(0)^3 + 7(0)^2 + 8 \\ &= 0 + 0 + 8 = 8 \text{ Ans.} \end{aligned}$$

For $y = -1$,

$$\begin{aligned} 2y^3 - 7y^2 + 8 &= 2(-1)^3 - 7(-1)^2 + 8 \\ &= -2 - 7 + 8 \\ &= -9 + 8 = -1 \text{ Ans.} \end{aligned}$$

$$(iv) \quad ab(a + ab + abc) = a^2b + a^2b^2 + a^2b^2c$$

For $a = 2, b = 1, c = 0$,

$$\begin{aligned} & a^2b + a^2b^2 + a^2b^2c \\ &= (2)^2 \times 1 + (2)^2 \times (1)^2 + (2)^2 \times (1)^2 \times (0) \\ &= 4 + 4 + 0 = 8 \text{ Ans.} \end{aligned}$$

Q. 5. Add :

$$(i) \quad x(x - y), y(y - z) \text{ and } z(z - x)$$

$$(ii) \quad 2x(x - y - z) \text{ and } 2y(z - y - x)$$

$$\text{Ans. } (i) \quad x(x - y) = x^2 - xy$$

$$y(y - z) = y^2 - yz$$

$$z(z - x) = z^2 - zx$$

Now, add

$$\begin{array}{r} x^2 - xy \\ + y^2 - yz \\ \hline x^2 - xy + y^2 - yz \end{array} \quad \begin{array}{r} + z^2 - zx \\ \hline + z^2 - zx \text{ Ans.} \end{array}$$

$$(ii) \quad 2x(x - y - z) = 2x^2 - 2xy - 2xz$$

$$\text{and } 2y(z - y - x) = 2yz - 2y^2 - 2xy$$

Now, add

$$\begin{array}{r} 2x^2 - 2xy - 2xz \\ - 2xy \quad + 2yz - 2y^2 \\ \hline 2x^2 - 4xy - 2xz + 2yz - 2y^2 \end{array} \quad \text{Ans.}$$

Q. 6. Subtract :

- (i) $8l(l - 4m + 5n)$ from $9l(10n - 3m + 2l)$
- (ii) $2a(a + b - c) - 2c(a + b - c)$ from $2c(-a + b + c)$

Solution.

$$(i) \quad 8l(l - 4m + 5n) = 8l^2 - 32lm + 40ln \quad \dots(i)$$

$$9l(10n - 3m + 2l) = 90ln - 27lm + 18l^2 \quad \dots(ii)$$

Now, subtract (i) from (ii)

$$\begin{array}{r} 18l^2 + 90ln - 27lm \\ 8l^2 + 40ln - 32lm \\ \hline 10l^2 + 50ln + 5lm \end{array} \text{ Ans.}$$

$$(ii) \quad 2a(a + b - c) - 2c(a + b - c)$$

$$= 2a^2 + 2ab - 2ac - 2ac - 2bc + 2c^2 \quad \dots(i)$$

$$= 2a^2 + 2ab - 4ac - 2bc + 2c^2 \quad \dots(ii)$$

$$2c(-a + b + c) = -2ac + 2bc + 2c^2 \quad \dots(ii)$$

Now, subtract (i) from (ii)

$$\begin{array}{r} -2ac + 2bc + 2c^2 \\ -4ac - 2bc + 2c^2 + 2a^2 + 2ab \\ + + - - - \\ \hline 2ac + 4bc + 0 - 2a^2 - 2ab \\ \\ = 4bc - 2ab + 2ac - 2a^2 \text{ Ans.} \end{array}$$

Q. 7. Subtract sum of $x(2x + 7) - 2$ and $3x$

($x - 2$) + 7 from $7x - 1$.

Solution.

$$x(2x + 7) - 2 = 2x^2 + 7x - 2 \quad \dots(i)$$

$$\text{and } 3x(x - 2) + 7 = 3x^2 - 6x + 7 \quad \dots(ii)$$

Add (i) and (ii)

$$\begin{array}{r} 2x^2 + 7x - 2 \\ 3x^2 - 6x + 7 \\ \hline 5x^2 + x + 5 \end{array}$$

Subtract $5x^2 + x + 5$ from $7x - 1$

$$\begin{array}{r} 7x - 1 \\ 5x^2 + x + 5 \\ - - - \\ \hline -5x^2 + 6x - 6 \end{array} \text{ Ans.}$$

Q. 8. Add $2xy(x + y + z)$ and $3y(x^2 - xy + xz)$ then subtract from $5x(xy + y^2 - 4yz)$.

Solution.

$$2xy(x + y + z) = 2x^2y + 2xy^2 + 2xyz \quad \dots(i)$$

$$3y(x^2 - xy + xz) = 3x^2y - 3xy^2 + 3xyz \quad \dots(ii)$$

Adding (i) and (ii)

$$\begin{array}{r} 2x^2y + 2xy^2 + 2xyz \\ 3x^2y - 3xy^2 + 3xyz \\ \hline 5x^2y - xy^2 + 5xyz \end{array} \quad \dots(iii)$$

$$5x(xy + y^2 - 4yz) = 5x^2y + 5xy^2 - 20xyz \quad \dots(iv)$$

Now, subtract (iii) from (iv)

$$\begin{array}{r} 5x^2y + 5xy^2 - 20xyz \\ 5x^2y - xy^2 + 5xyz \\ - + - \\ \hline 6xy^2 - 25xyz \end{array} \text{ Ans.}$$

Q. 9. Multiple Choice Questions :

- (i) Product of pqr and $p + q + r$ will be :

- (a) pqr
- (b) $p^2qr + pq^2r + pqr^2$
- (c) $pq + qr + pr$
- (d) $p^2qr + pqr^2$.

- (ii) Find value of $x^2 + x$ at $x = 2$.

- (a) 4
- (b) 6
- (c) 8
- (d) 10.

- (iii) Find $y \times y^2 \times y^3 \times y^4$

- (a) y
- (b) y^6
- (c) y^{10}
- (d) y^{25} .

- (iv) Find the product of $xy + 4z + 3x$ with 0.

- (a) $xy + yz + 3x$
- (b) xyz
- (c) 0
- (d) $x^2y^2z^2$.

Ans. (i) (b) $p^2qr + pq^2r + pqr^2$

(ii) (b) 6

(iii) (c) y^{10} (iv) (c) 0.