

TEXT BOOK EXERCISE 6.4

Q. 1. Cube of a number is 64. Find the number.

Solution. Let the number = x

Its Cube = $x \times x \times x = x^3$

$$\therefore x^3 = 64 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2}$$

$$\sqrt[3]{x^3} = \sqrt[3]{2 \times 2 \times 2 \times 2 \times 2 \times 2}$$

$$\Rightarrow x = 2 \times 2 = 4$$

2	64
2	32
2	16
2	8
2	4
2	2
	1

Hence, the required number is 4 Ans.

Q. 2. Cube of a number is 3375. Find the number.

Solution. Let the number = x

$$\text{Its cube} = x^3$$

$$\therefore x^3 = 3375 = \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$$

$$\sqrt[3]{x^3} = \sqrt[3]{3 \times 3 \times 3 \times 5 \times 5 \times 5}$$

$$\Rightarrow x = 3 \times 5 = 15$$

3	3375
3	1125
3	375
5	125
5	25
5	5
	1

Hence, the required number = 15 Ans.

Q. 3. Find the cube root of each of the following numbers by prime factorisation :

$$(i) 5832 \quad (ii) 216000$$

$$(iii) 456533 \quad (iv) 729000$$

$$(v) 85184 \quad (vi) 328509$$

Solution. (i) Let us find prime factorisation of 5832.

2	5832
2	2916
2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

The prime factorisation of 5832 is :

$$5832 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \times \underline{3 \times 3 \times 3}$$

$$\text{Hence, } \sqrt[3]{5832} = \sqrt[3]{2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3}$$

$$= 2 \times 3 \times 3$$

$$= 18 \text{ Ans.}$$

(ii) Let us find prime factorisation of 216000

2	216000
2	108000
2	54000
2	27000
2	13500
2	6750
3	3375
3	1125
3	375
5	125
5	25
5	5
	1

The prime factorisation of 216000 is :

$$216000 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$$

$$\text{Hence, } \sqrt[3]{216000}$$

$$= \sqrt[3]{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5 \times 5} \\ = 2 \times 2 \times 3 \times 5 = 60 \text{ Ans.}$$

(iii) Let us find prime factorisation of 456533.

7	456533
7	65219
7	9317
11	1331
11	121
11	11
	1

The prime factorisation of 456533 is :

$$456533 = \underline{7 \times 7 \times 7} \times \underline{11 \times 11 \times 11}$$

$$\text{Hence, } \sqrt[3]{456533} = \sqrt[3]{7 \times 7 \times 7 \times 11 \times 11 \times 11} \\ = 7 \times 11 = 77 \text{ Ans.}$$

(v) Let us find prime factorisation of 729000.

2	729000
2	364500
2	182250
3	91125
3	30375
3	10125
3	3375
3	1125
3	375
5	125
5	25
5	5
	1

The prime factorisation of 729000 is :

$$729000 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \\ \times \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$$

Hence, $\sqrt[3]{729000}$

$$= \sqrt[3]{2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 5 \times 5 \times 5} \\ = 2 \times 3 \times 3 \times 5 = 90 \text{ Ans.}$$

(vi) Let us find prime factorisation of 85184.

2	85184
2	42592
2	21296
2	10648
2	5324
2	2662
11	1331
11	121
11	11
	1

The prime factorisation of 85184 is :
 $85184 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{11 \times 11 \times 11}$

Hence, $\sqrt[3]{85184}$

$$= \sqrt[3]{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 11 \times 11 \times 11} \\ = 2 \times 2 \times 11 = 44 \text{ Ans.}$$

(vi) Let us find prime factorisation of 328509.

3	328509
3	109503
3	36501
23	12167
23	529
23	23
	1

The prime factorisation of 328509 is :

$$328509 = \underline{3 \times 3 \times 3} \times \underline{23 \times 23 \times 23}$$

$$\text{Hence, } \sqrt[3]{328509} = \sqrt[3]{3 \times 3 \times 3 \times 23 \times 23 \times 23} \\ = 3 \times 23 = 69 \text{ Ans.}$$

Q. 4. Multiple Choice Questions :

(i) What is cube root of 512 ?

- (a) 2 (b) 4
 (c) 6 (d) 8.

(ii) Find $\sqrt[3]{1728}$.

- (a) 10 (b) 12
 (c) 14 (d) 16.

(iii) Find cube root of 1331.

- (a) 11 (b) 21
 (c) 31 (d) 23.

(iv) A perfect cube ends with digit 2. What will be ones digit of its cube root ?

- (a) 4 (b) 2
 (c) 6 (d) 8.

Ans. (i) (d) 8 (ii) (b) 12
 (iii) (a) 11 (iv) (d) 8.

Objective Type Questions

Multiple Choice Questions :

(i) What is the digit at the unit's place of the cube of 243 ?

- (a) 3 (b) 9
 (c) 7 (d) 6.

Ans. (c) 7.

(ii) Which of the following does not represent the factors of a perfect cube number ?

- (a) $2 \times 2 \times 2 \times 3 \times 3 \times 3$
 (b) $4 \times 4 \times 4 \times 4 \times 4 \times 4 \times 5 \times 5 \times 5$
 (c) $6 \times 6 \times 6 \times 5 \times 5 \times 5 \times 5 \times 5 \times 5 \times 5$
 (d) $2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5 \times 5$.

Ans. (c) $6 \times 6 \times 6 \times 5 \times 5 \times 5 \times 5 \times 5 \times 5$.

- (iii) Find the smallest number by which 192 be divided to make it a perfect cube.
- (a) 2 (b) 3
 (c) 5 (d) 6.

Ans. (a) 2.

- (iv) How many perfect cube numbers are there from 1 to 1000 ?
- (a) 9 (b) 10
 (c) 11 (d) 12.

Ans. (b) 10.

- (v) Observe the following pattern and fill in the blanks :

$$2^3 - 1^3 = 1 + 2 \times 1 \times 3$$

$$3^3 - 2^3 = 1 + 3 \times 2 \times 3$$

$$4^3 - 3^3 = 1 + 4 \times 3 \times 3$$

$$12^3 - 11^3 = \dots$$

- (a) $1 + 11 \times 12 \times 4$
 (b) $1 + 12 + 11 \times 4$
 (c) $1 + 12 \times 11 \times 3$
 (d) $1 + 12 \times 11 \times 5$.

Ans. (a) $1 + 12 \times 11 \times 3$.

- (vi) Find the cube root of 8000.
- (a) 40 (b) 80
 (c) 20 (d) 400.

Ans. (c) 20.

- (vii) If $53240 = 2 \times 2 \times 2 \times 11 \times 11 \times 5$ then with which number 53240 is to multiply ?

- (a) 5 (b) 25
 (c) 15 (d) 22.

Ans. (b) 25.

- (viii) Which of the following statement is true ?
- (a) The cube of an even number is an odd number
 (b) The cube of an odd number is an odd number
 (c) A perfect cube ends with two zeroes
 (d) The cube of a single digit number is always a single digit.

Ans. (b) The cube of an odd number is an odd number.

- (ix) Cube root of 125 is :
- (a) 1 (b) 3
 (c) 5 (d) 7.

Ans. (c) 5.

- (x) What is the number of zeroes at the end of a perfect cube ?

- (a) 1 (b) 2
 (c) 3 (d) 4.

Ans. (c) 3.

2. Choose True/False for the following questions :

- (i) 1729 has been known as the Hardy-Ramanjan Number. (True/False)

Ans. True.

- (ii) 125 is a cube number. (True/False)

Ans. True.

- (iii) Perfect cube can have 1,4,5,6,7,9 in the ones place. (True/False)

Ans. True.

- (iv) Cube root of 343 is 9. (True/False)

Ans. False.

- (v) Volume of cube with side 15 cm is 227 cm³. (True/False)

Ans. False.

3. Fill in the blanks :

- (i) Numbers obtained when a number is multiplied by itself three times are known as numbers.

Ans. cube.

- (ii) The symbol $\sqrt[3]{\quad}$ denotes

Ans. cube roots.

- (iii) 27 is a perfect number.

Ans. cube.

- (iv) A cube can have zero at its end.

Ans. three.

- (v) A ones digit number can have digit.

Ans. one.